Model Reduction Across Disciplines, 19-22 August 2014 University of Leicester

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# When are Two Eyes Better than One: Model Construction vs Model Reduction

### Rutherford Aris (1929 – 2005)



# The most remarkable coincidence in my life

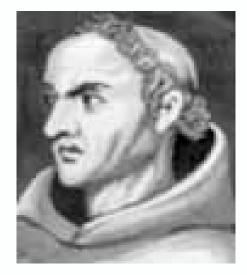
## • "TWO EYES ARE BETTER THAN ONE:

- some reflections on the importance to have more than one viewpoint in mathematical disciplines or other disciplines",
- *Mathl. Comput.Modelling*, Vol.18, No.8, pp. 95-113, 1993

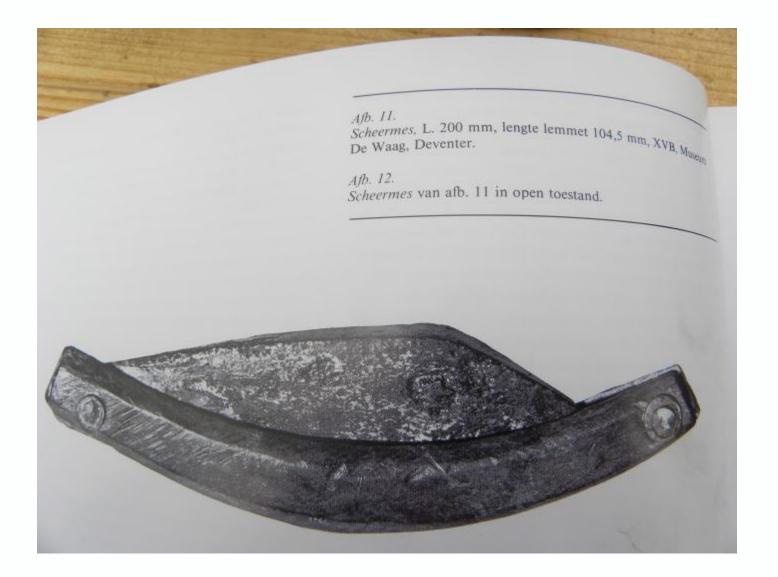
#### Pomona, the Roman Goddess of Fruitful Abundance



# William of Occam (1288-1348)



#### Occam's razor



#### Occam's Razor

# Entia non sunt multiplicanda praeter necessitatem

- (entities must not be multiplied beyond necessity)
- These words attributed to Ockham are absent in his extant works

#### Bonsai Tree as a Model



#### **Origami Bonsai Tree as a Ideal Scientific Model**



## Outline

- Introduction
- Concepts and experimental devices
- Models
- Chemical Calculus:
- TAP-experiments and data analysis
- CO oxidation
- Conclusions

Reaction mechanism or mechanism:

- Fundamental concept of chemical kinetics
- Comprehensive interpretation of all experimental data accumulated on a complex reaction process
- Includes a detailed description of the steps leading from the reactants to the products of a reaction

*G.B. Marin & G.S. Yablonsky (2011).*  **Oxydation of Hydrogen** 

# $2 H_2 + O_2 \implies 2 H_2 O$

- 5 intermediates:  $H_{\cdot}$ ,  $O_{\cdot}$ ,  $OH_{\cdot}$ ,  $HO_{2}$ ,  $H_{2}O_{2}$
- 30 elementary steps

*G.B. Marin & G.S. Yablonsky (2011).* <sup>13</sup>

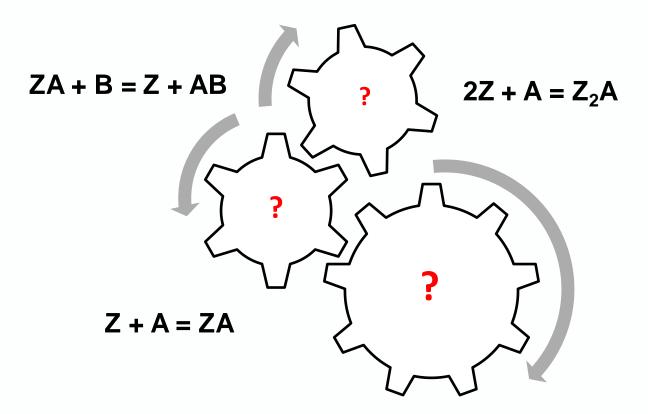
# Chemical Kinetics Textbook Knowledge (3)

•Detailed mechanism is a set of elementary reactions which law is assumed , e. g. the mass-action-law

#### •An example: Hydrogen Oxidation 2H<sub>2</sub> +O<sub>2</sub> = 2H<sub>2</sub>O

•1)  $H_2 + O_2 = 2 OH$ ; 2)  $OH + H_2 = H_2O + H$ ; 3)  $H + O_2 = OH + O$ ; •4)  $O + H_2 = OH + H$ ; 5)  $O + H_2O = 2OH$ ; 6)  $2H + M = H_2 + M$ ; 7)  $2O + M = O_2 + M$ ; •8)  $H + OH + M = H_2O + M$ ; 9)  $2 OH + M = H_2O_2 + M$ ; 10)  $OH + O + M = HO_2 + M$ ; •11)  $H + O_2 + M = HO_2 + M$ ; 12)  $HO_2 + H_2 = H_2O_2 + H$ ;13)  $HO_2 + H_2 = H_2O + OH$ ; •14)  $HO_2 + H_2O = H_2O_2 + OH$ ; 15)  $2HO_2 = H_2O_2 + O_2$ ; 16)  $H + HO_2 = 2 OH$ ; •17)  $H + HO_2 = H_2O + O$ ; 18)  $H + HO_2 = H_2 + O_2$ ; 19)  $O + HO_2 = OH + H$ ; •20)  $H + H_2O_2 = H_2O + OH$ ; 21)  $O + H_2O_2 = OH + HO_2$ ; 22)  $H_2 + O_2 = H_2O + O$ ; •23)  $H_2 + O_2 + M = H_2O_2 + M$ ; 24) OH + M = O + H + M; 25)  $HO_2 + OH = H_2O + O_2$ ; •26)  $H_2 + O + M = H_2O + M$ ; 27)  $O + H_2O + M = H_2O_2 + M$ ; 28)  $O + H_2O_2 = H_2O + O_2$ ; •29)  $H_2 + H_2O_2 = 2H_2O$ ; 30)  $H + HO_2 + M = H_2O_2 + M$ 

Catalyst and process design require **reliable microkinetic models** of catalytic reactions ...



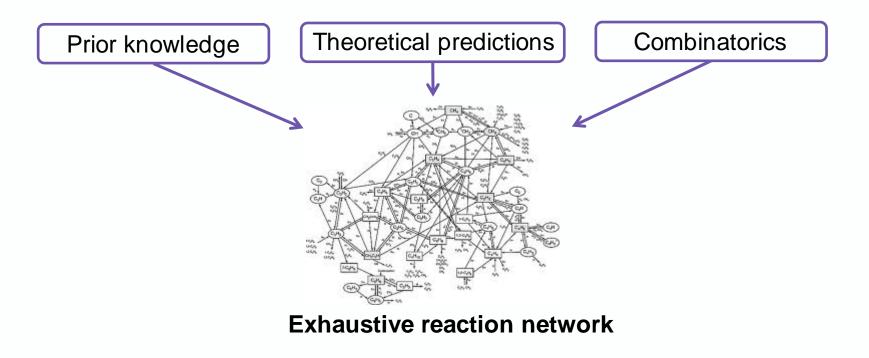
#### Methane Steam Reforming

**Overall reactions:**  $CH_4 + H_2O \implies CO + 3H_2$  $CO+H_2O \longrightarrow CO_2+H_2$ CH, (Z) (1)  $\leftarrow$   $CH_2Z + H_2$ active site  $CH_2Z+H_2O \longrightarrow CHOHZ+H_2$ (2) (3)CHOHZ  $\leftarrow$  COZ + H<sub>2</sub> (4)COZ  $\overrightarrow{\qquad}$  Z+CO (5)  $Z+H_2O \longrightarrow OZ+H_2$  $CO \longrightarrow Z + CO_2$ (6)surface intermediate

> G.B. Marin & G.S. Yablonsky (2011).

**16** 

Catalyst and process design require **reliable microkinetic models** of catalytic reactions ...



Which subset is kinetically important in my experiment?

Approaches to model discrimination:

- **Regression of data** using the entire network or multiple rival models.
- Search for kinetic fingerprints within the network and construction of minimal reaction mechanism.

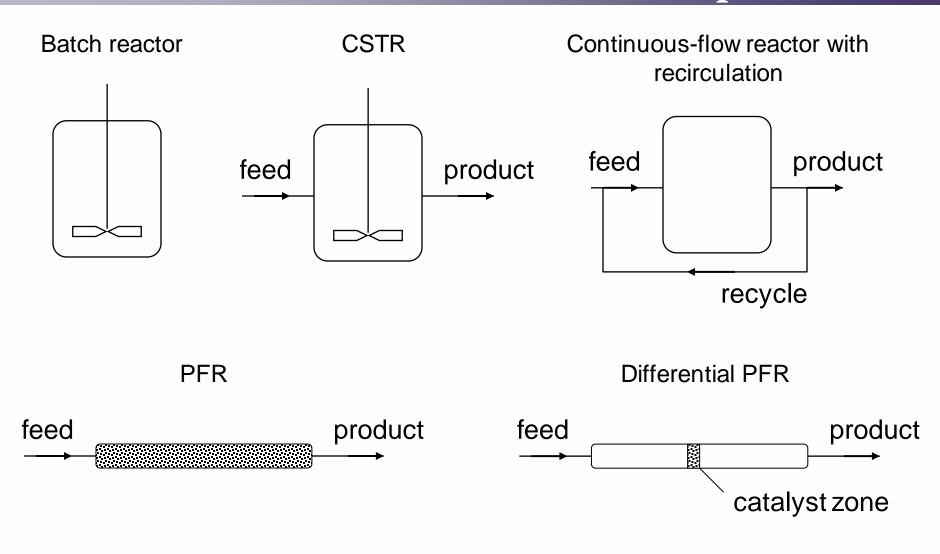
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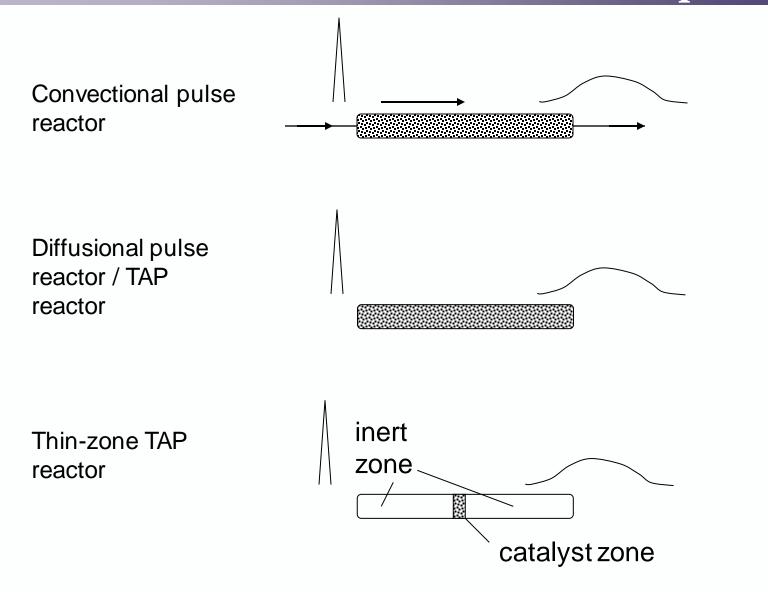
More tractable microkinetic models

#### **Reactors for Kinetic Experiments**



20 G.B. Marin & G.S. Yablonsky (2011) *Vinctics of Chaminal* 

#### **Reactors for Kinetic Experiments**



G.B. Marin & G.S. Yablonsky

# Non-Steady-State Models

$$\frac{d\boldsymbol{c}}{dt} = f\left(\boldsymbol{c}, \boldsymbol{k}\right)$$

describes the temporal evolution of a chemical reaction mixture from an initial state to a final state

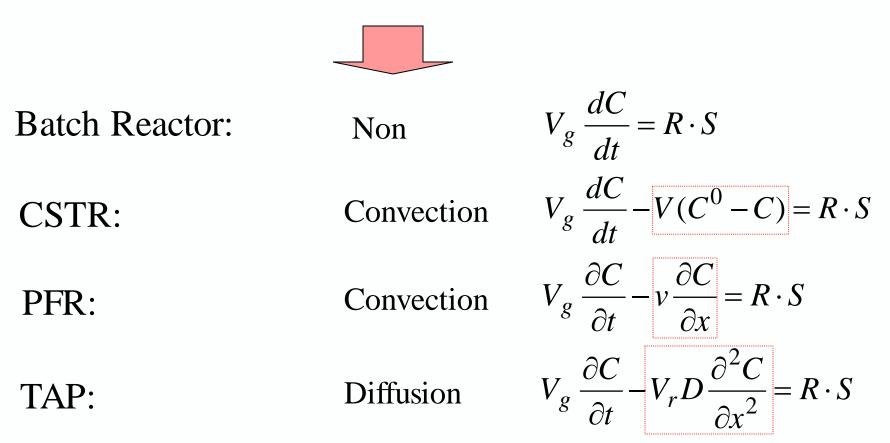
- closed system: equilibrium
- open system: steady state

Three methods for studying non-steady-state behavior:

- change in time *t*: change in dynamic space (*c*, *t*)
- change of parameters **k**: change in parametric space (**c**, **k**)
- change of a concentration with respect to others: change in phase space

## **Kinetic Model-Free Analysis**

**Reactor Model:** Accumulation - Transport Term = Reaction Rate

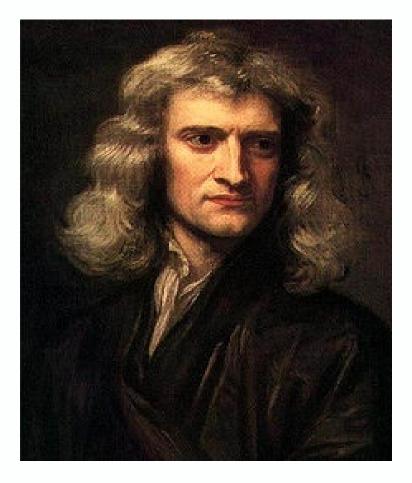


I. STOP TIME ! II. Chemical Calculus

# Founders of infinitesimal calculus: Newton and Leibnitz

In Europe, the foundational work was a treatise due to Bonaventura Cavalieri, who argued that volumes and areas should be computed as the sums of the volumes and areas of infinitesimal thin cross-sections

#### **Isaac Newton (1642-1727)**



#### **Gottfried Wilhelm Leibnitz (1646-1716)**

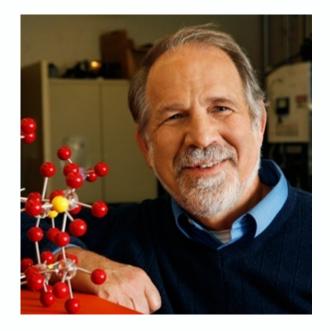


The origins of volumetric analysis are in late-18th-century French chemistry. Francois Antoine Henri Descroizilles developed the first burette (which looked more like a graduated cylinder) in 1791. Joseph Louis Gay-Lussac developed an improved version of the burette that included a side arm, and coined the terms "pipette" and "burette" in an 1824 paper on the standardization of indigo solutions

#### Manfred Eigen (1927): Chemical relaxation, but not calculus



#### **Experimental chemical calculus : John T. Gleaves**



## Temporal Analysis of Products (TAP), a vacuum transient response experiment performed by injecting a small number of gas molecules into an evacuated reactor containing a solid sample, which provides precise kinetic characterization of gassolid interactions with submillisecond time resolution (developed by J.T. Gleaves in 1988)

#### Non-Steady-State Catalytic Processes

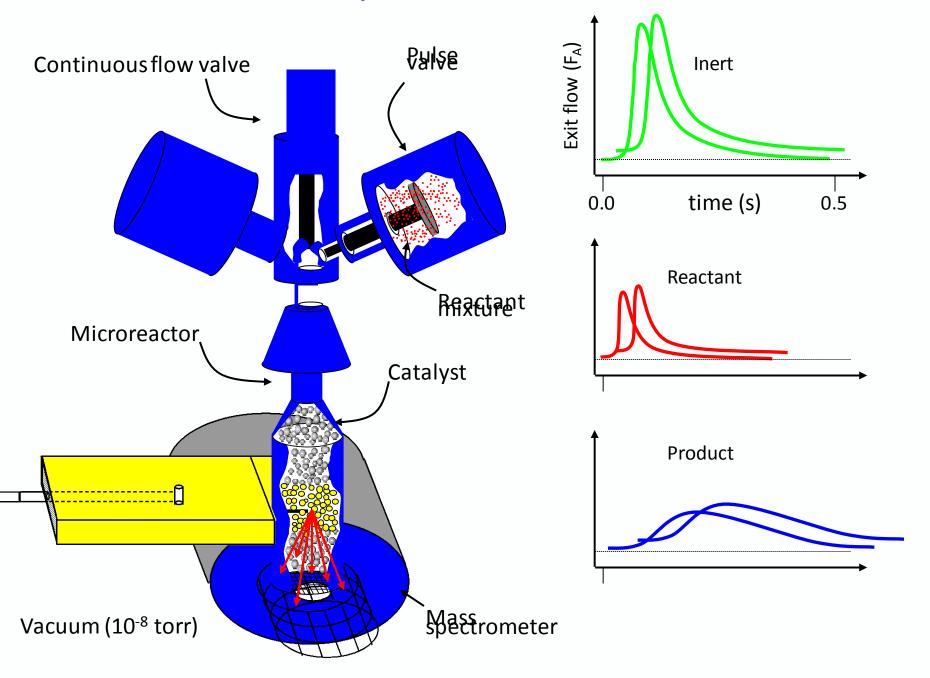
- Automotive catalytic processes
- Reverse-flow processes
- Oxidation-reduction processes for selective hydrocarbon oxidation
- Circulating fluidized-bed reactors
- Chemical looping combustion (CLC) (total oxidation of hydrocarbons by metal oxides)

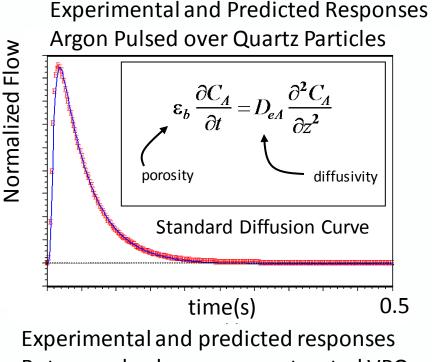
## Non-Steady-State Kinetic Screening

## TAP: Temporal Analysis of Products

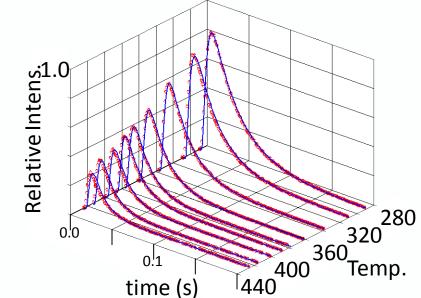
- Series of pulses of very small intensity
- Change of catalyst composition in controlled manner
- Sequence of *infinitesimal* steps produces a *finite* change → "chemical calculus"

#### TAP Reactor System-Overview

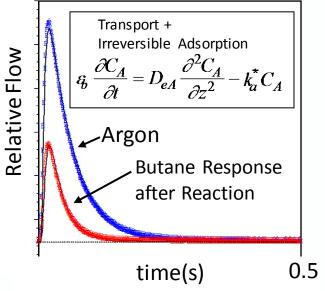




Butane pulsed over oxygen treated VPO

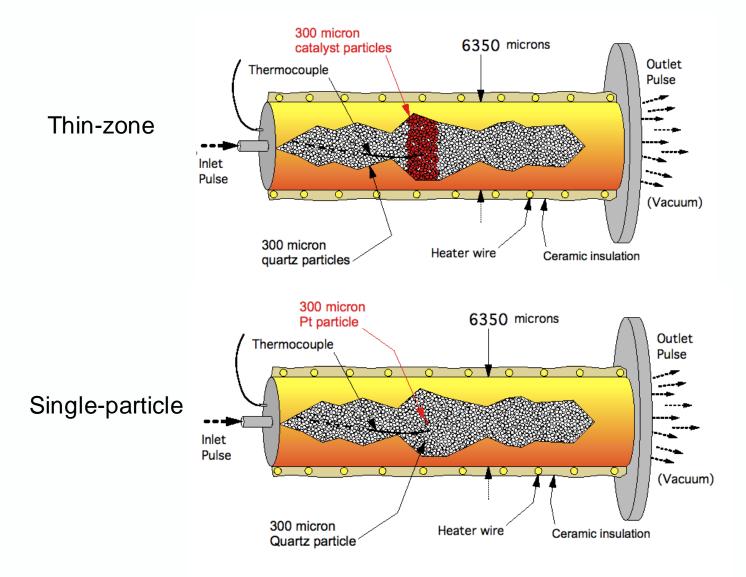


Experimental and Predicted Responses Argon and Butane Pulsed over VPO



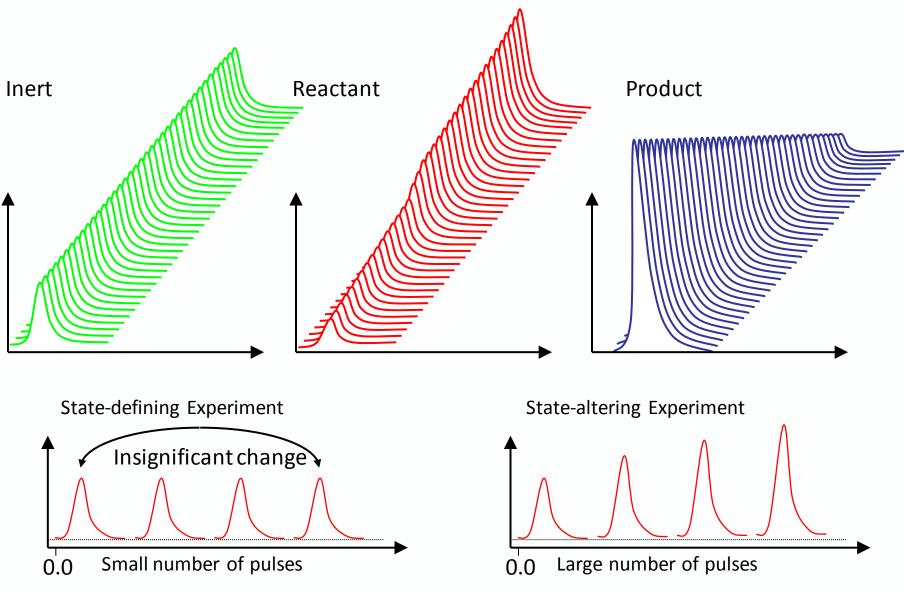
Non-uniformity along the catalyst bed was produced in multi-pulse experiment

### Thin-zone and Single Particle Reactor Configurations



#### TAP Multipulse Experiment Combines

State-Defining & State-Altering Experiment



# **Principles of the TAP-experiment**

- 3 principles:
- (1) Insignificant change of catalyst composition during the single pulse
- (2) Controlled change of catalyst composition during the series of pulses
- (3) Uniformity of the active zone regarding the composition

# And... Transport is well-defined: Knudsen diffusion

• Interrogative kinetics, a systematic approach combining small stepwise changes in catalyst surface composition with precise kinetic characterization after each change to elucidate the evolution of catalyst properties and provide information on the relationship between surface composition and kinetic properties. (developed by J.T. Gleaves and G. Yablonsky in 1997)

### **Interrogative Kinetics (IK) Approach**

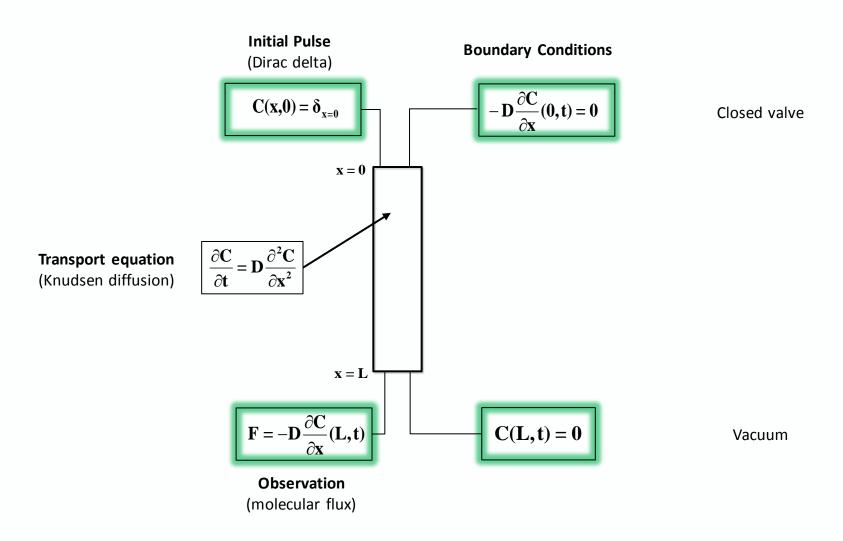
Was firstly introduced in the paper: Gleaves, J.T., Yablonskii, G.S., Phanawadee, Ph., Schuurman, Y. "TAP-2: An Interrogative Kinetics Approach" *Appl. Catal.*, A: General, 160 (1997) 55.

The main idea is to combine two types of experiments:

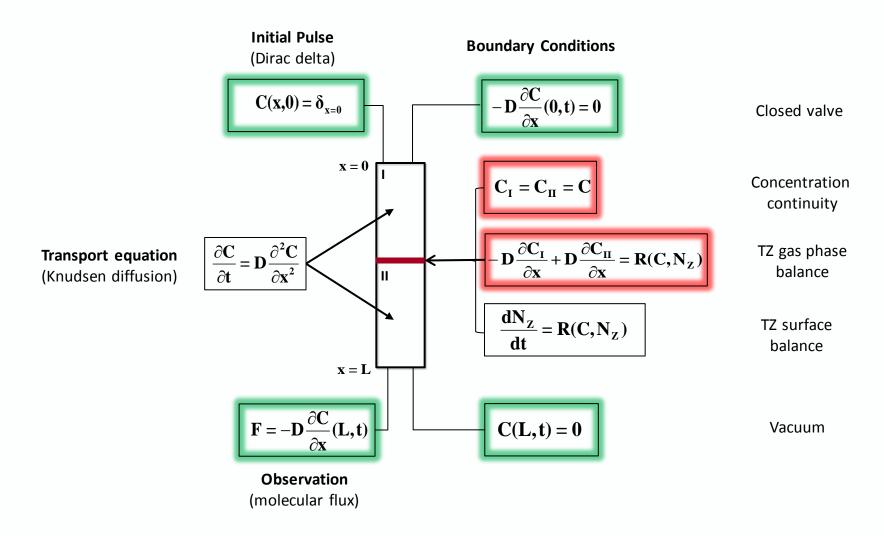
A state-defining experiment in which the catalyst composition and structure change insignificantly during a kinetic test

A state-altering experiment in which the catalyst composition is changed in a controlled manner

# One zone: the diffusion equation requires an initial condition and two boundary conditions (as a second order PDE)



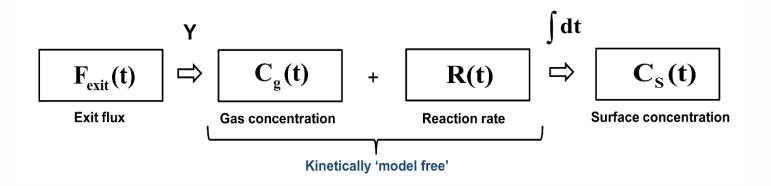
#### Two zones: each zone requires two boundary conditions



G. S. Yablonsky, D. Constales, et. al., Chem. Eng. Sci., 62, 6754 (2007)

- 1. exact solution in the Laplace domain;
- 2. switching to the Fourier domain to allow sufficient computation;
- 3. introduction to discretization and filtering in the Fourier domain to deal with the real data (in the time domain) subject to noise.

Transposition to the Fourier domain combined with time discretization and filtering of the highfrequency noise leads to an efficient practical method for the reconstruction of gas-phase concentrations in a non-steady-state regime without any presuppositions about the kinetic dependence, that is, it is a model-free procedure. The Y-Procedure analysis provides us with:

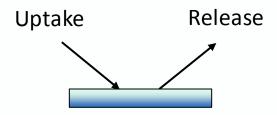


- 'Model free' transient kinetics
- Millisecond time resolution
- For complex multicomponent catalysts
- At the upper limit of the surface science range (10<sup>-6</sup> torr)
- Keeping high spacial uniformity for conversions up to 80% [1]

#### How do we deal with this information?

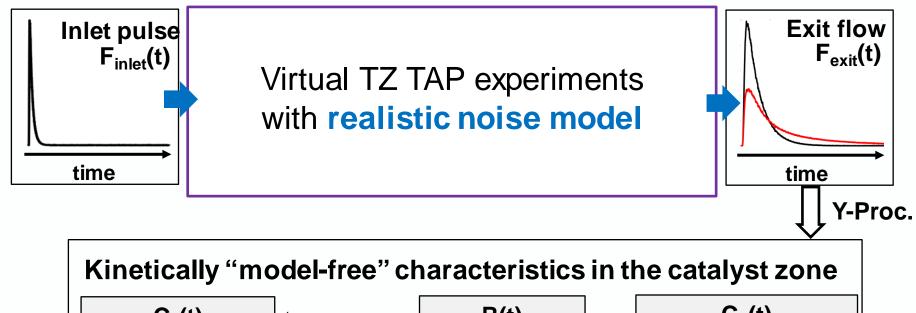
[1] - S. Shekhtman, et. al., Chem. Eng. Sci., 59, 5493 (2004)

Calculating surface concentrations (instantaneous storages) as a transient difference between total uptake and release



$$\mathbf{C}_{\mathbf{S}}(t) = \mathbf{Uptake}(t) - \mathbf{Release}(t) = \int_{0}^{t} \sum_{i} \mathbf{v}_{i} \mathbf{R}_{i}(\tau) d\tau$$

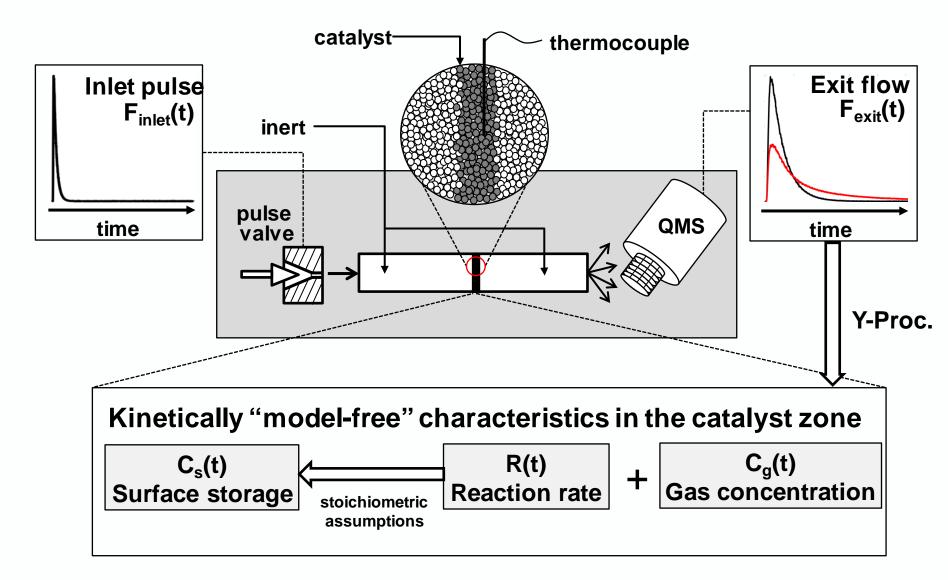
### Thin-Zone (TZ) Temporal Analysis of Products (TAP)



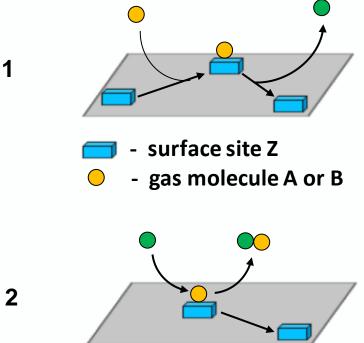
$$C_{ZCO}(t) = C_{ZCO,init} + \int_0^t R_{CO}(t')dt' - \int_0^t R_{CO_2}(t')dt'$$

$$C_{ZO}(t) = C_{ZO,init} + \int_0^t 2R_{O_2}(t')dt' - \int_0^t R_{CO_2}(t')dt'$$

### Thin-Zone (TZ) Temporal Analysis of Products (TAP)



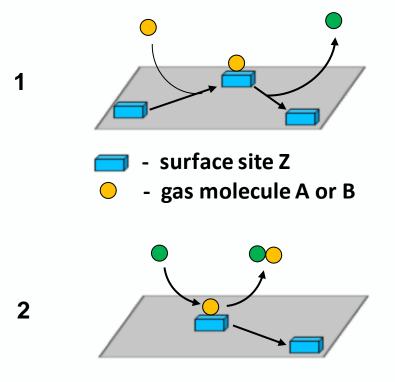
### **Communication between gas and surface phases**



Molecular adsorption:	Z + A = ZA
Dissociative adsorption:	2Z + A = 2ZA
Product release:	ZA = Z + B

Impact reaction steps: ZA + B = Z + AB

### Communication between gas and surface phases



Molecular adsorption:	Z + A = ZA
Dissociative adsorption:	2Z + A = 2ZA
Product release:	ZA = Z + B

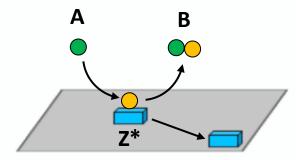
Impact reaction	steps:	ZA + B = Z + AB
-----------------	--------	-----------------



'Hidden' surface steps:	ZA + ZB = Z + ZC
	ZA = ZC
	ZA + Z = Z₂A

# **Testing kinetic coherency**

**Kinetic coherency** – Every combination of elementary steps leads to synchronization of certain kinetic characteristics



#### Rate-Rate coherency:

If A is consumed and B is produced in the same step, their rates must be synchronized (equal in this case):

 $R_A(t) = R_B(t)$ 

#### **Rate-Concentration coherency:**

Assuming the law of mass actions is valid, certain combinations of rates and concentrations must be synchronized, e.g:

 $R_{AB}(t) / C_{A}(t)C_{Z^{*}}(t) \neq f(t)$ 

#### **Elementary steps:**

- (1)  $O_2 + 2Z \rightarrow 2ZO$
- (2)  $CO + Z \leftrightarrow ZCO$
- $(3) \qquad \text{CO} + \text{ZO} \rightarrow \text{Z} + \text{CO}_2$
- $(4) \qquad \text{ZCO} + \text{ZO} \rightarrow 2\text{Z} + \text{CO}_2$
- (5)  $ZO + Z_b \rightarrow Z + Z_bO$

### Eley-Rideal (ER):

- (1)  $O_2 + 2Z \rightarrow 2ZO$
- $(2) \qquad CO + Z \leftrightarrow ZCO$
- $(3) \qquad \text{CO} + \text{ZO} \rightarrow \text{Z} + \text{CO}_2$
- $(4) \qquad ZCO + ZO \rightarrow 2Z + CO_2$
- $(5) \qquad ZO + Z_b \rightarrow Z + Z_bO$

#### Langmuir-Hinshelwood (LH):

- (1)  $O_2 + 2Z \rightarrow 2ZO$
- (2)  $CO + Z \leftrightarrow ZCO$
- $(3) \qquad \mathsf{CO} + \mathsf{ZO} \to \mathsf{Z} + \mathsf{CO}_2$
- $(4) \qquad \text{ZCO} + \text{ZO} \rightarrow 2\text{Z} + \text{CO}_2$

 $(5) \qquad ZO + Z_b \rightarrow Z + Z_bO$ 

#### Combined (ER+LH):

- (1)  $O_2 + 2Z \rightarrow 2ZO$
- (2)  $CO + Z \leftrightarrow ZCO$
- $(3) \qquad \text{CO} + \text{ZO} \rightarrow \text{Z} + \text{CO}_2$
- $(4) \qquad ZCO + ZO \rightarrow 2Z + CO_2$

 $(5) \qquad ZO + Z_b \to Z + Z_bO$ 

#### **Buffer Step (ER+BS):**

- (1)  $O_2 + 2Z \rightarrow 2ZO$
- (2)  $CO + Z \leftrightarrow ZCO$
- $(3) \qquad \text{CO} + \text{ZO} \rightarrow \text{Z} + \text{CO}_2$
- $(4) \qquad ZCO + ZO \rightarrow 2Z + CO_2$
- $(5) \qquad ZO + Z_b \rightarrow Z + Z_bO$

#### Additional Oxygen Process (ER+AOP):

- (1)  $O_2 + 2Z \rightarrow 2ZO$
- $(2) \qquad CO + Z \leftrightarrow ZCO$
- $(3) \qquad \text{CO} + \text{ZO} \rightarrow \text{Z} + \text{CO}_2$
- $(4) \qquad \text{ZCO} + \text{ZO} \rightarrow 2\text{Z} + \text{CO}_2$
- (5)  $ZO + Z_b \rightarrow Z + Z_bO$

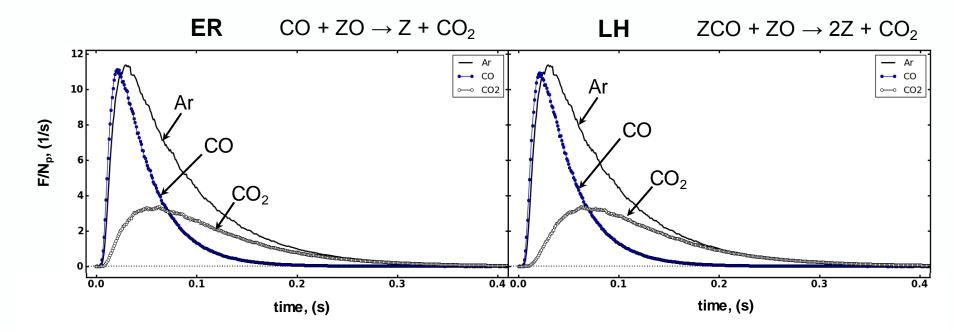
#### **Elementary steps:**

- (1)  $O_2 + 2Z \rightarrow 2ZO$
- (2)  $CO + Z \leftrightarrow ZCO$
- $(3) \qquad \text{CO} + \text{ZO} \rightarrow \text{Z} + \text{CO}_2$
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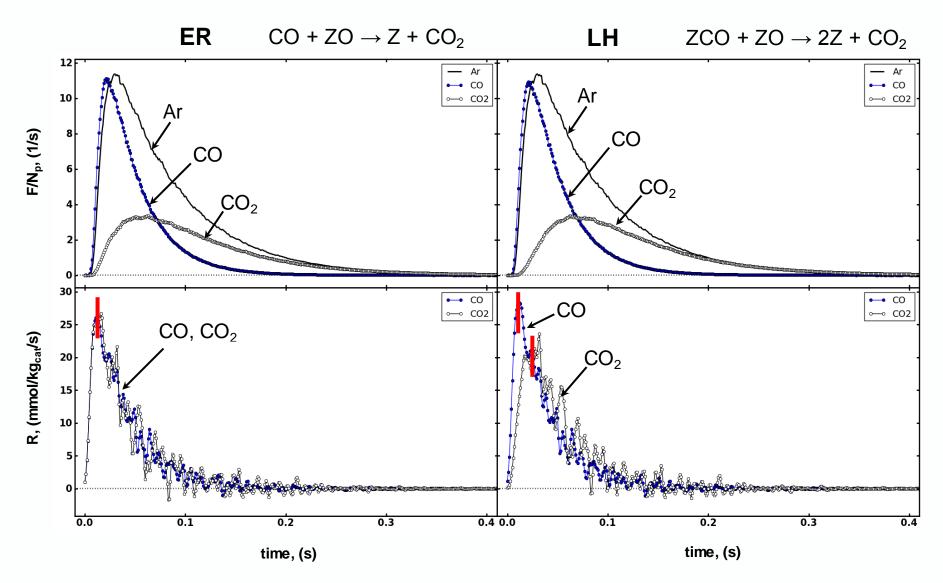
#### **Possible mechanisms:**

- [1] ER [2] LH
- [3] ER+LH
  - [4] ER+BS
  - [5] ER+AOP
  - [6] LH+AOP
  - [7] ER+BS+AOP
  - [8] ER+LH+AOP

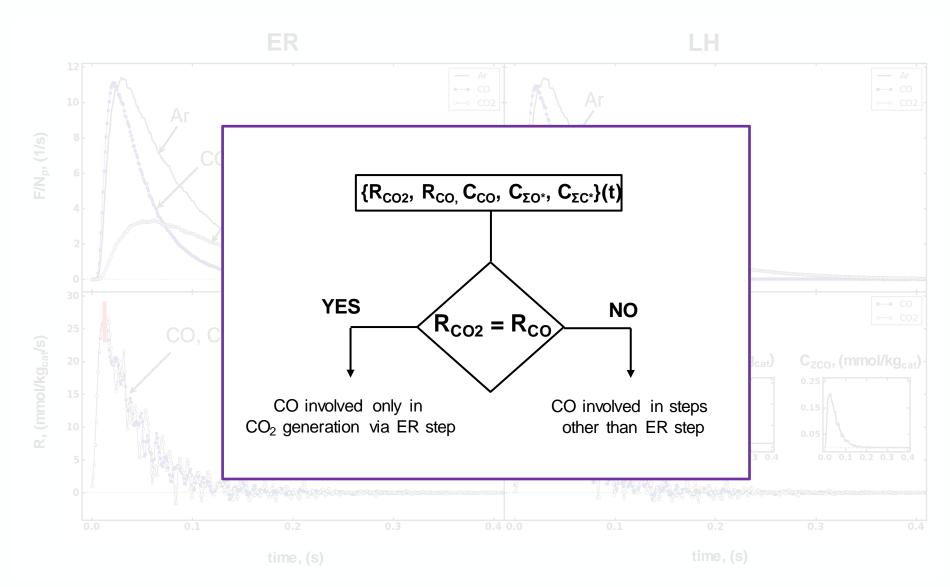
### **Rate-Rate coherency**



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### **Rate-Rate coherency**



Is CO<sub>2</sub> formed **only** through ER step or(also) through LH steps?

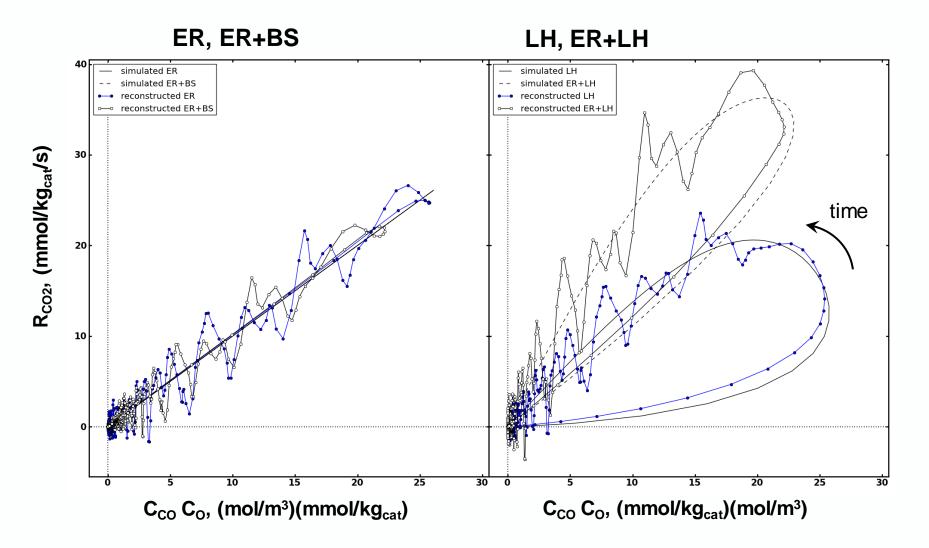
**ER, ER+BS**: 
$$R_{CO_2} = k^{ER} C_{ZO} C_{CO}$$

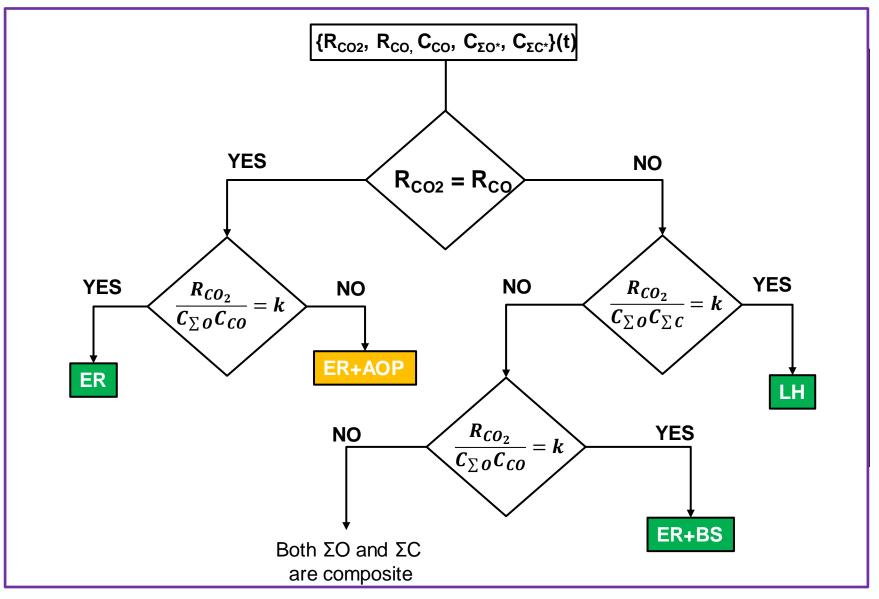
Is CO<sub>2</sub> formed **only** through ER step or(also) through LH steps?

**ER, ER+BS**: 
$$R_{CO_2} = k^{ER} C_{ZO} C_{CO}$$

Data should give a linear plot in these coordinates ...

... unless other steps are involved.





Is CO<sub>2</sub> formed **only** through a combined ER+LH mechanism or other processes are also involved?

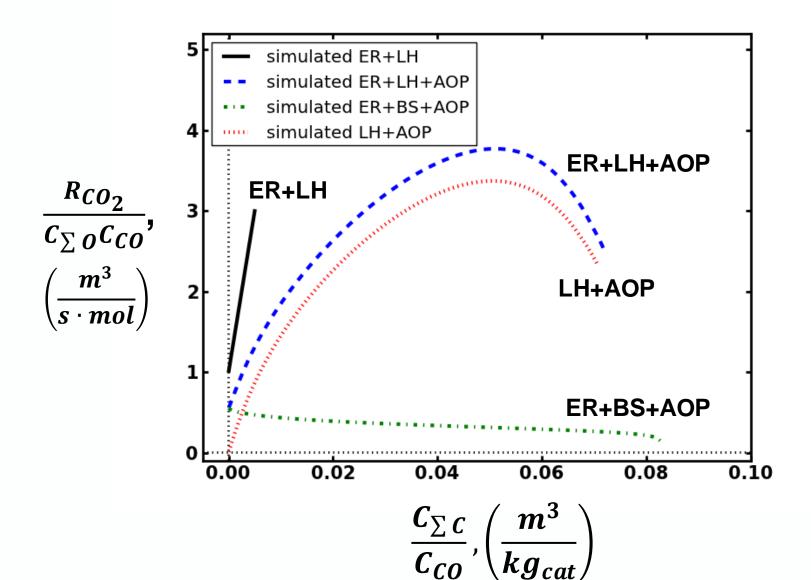
**ER+LH**: 
$$R_{CO_2} = k^{ER} C_{ZO} C_{CO} + k^{LH} C_{ZO} C_{ZCO}$$

Is CO<sub>2</sub> formed **only** through a combined ER+LH mechanism or other processes are also involved?

**ER+LH**: 
$$R_{CO_2} = k^{ER} C_{ZO} C_{CO} + k^{LH} C_{ZO} C_{ZCO}$$
  
$$\frac{R_{CO_2}}{C_{ZO} C_{CO}} = k^{ER} + k^{LH} \frac{C_{ZCO}}{C_{CO}}$$

Data should give a linear plot in these coordinates ...

... unless other steps are involved.



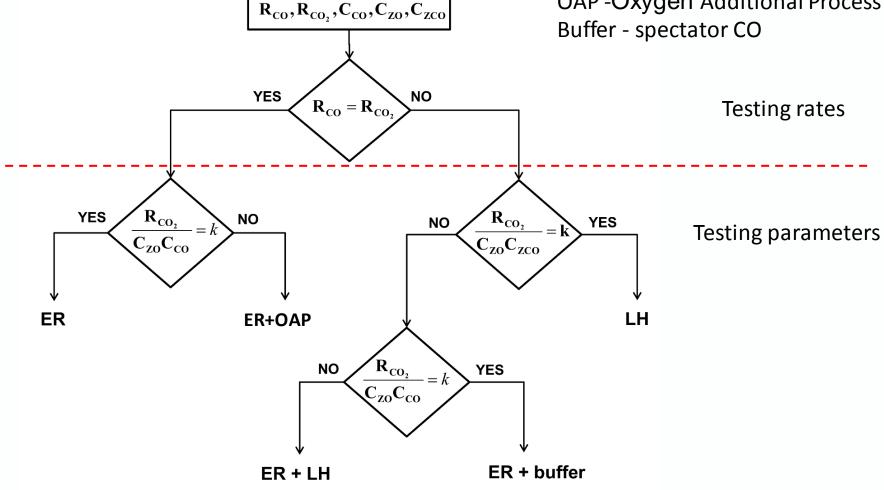
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# Decision tree in determining mechanisms for oxygen pre-covered surface

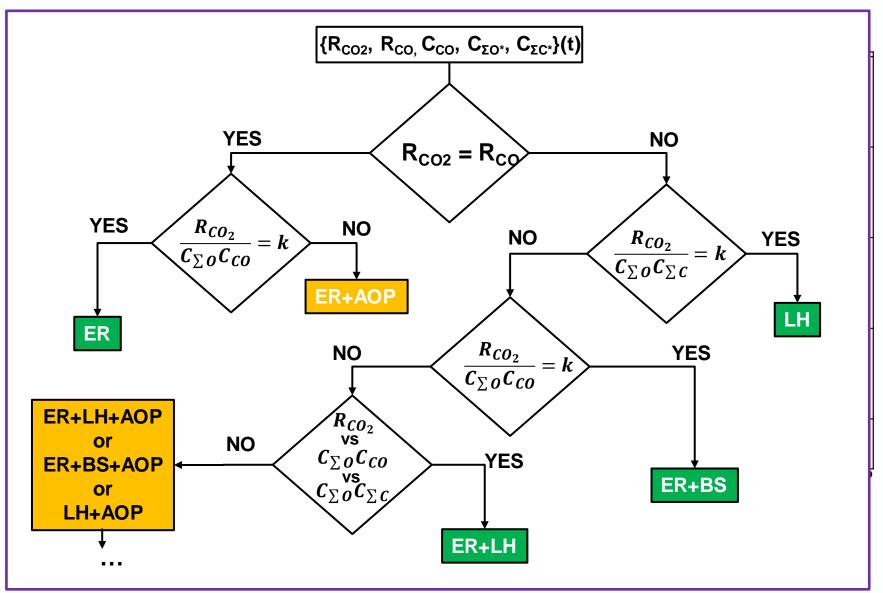
Legend:

ER - Eley-Rideal

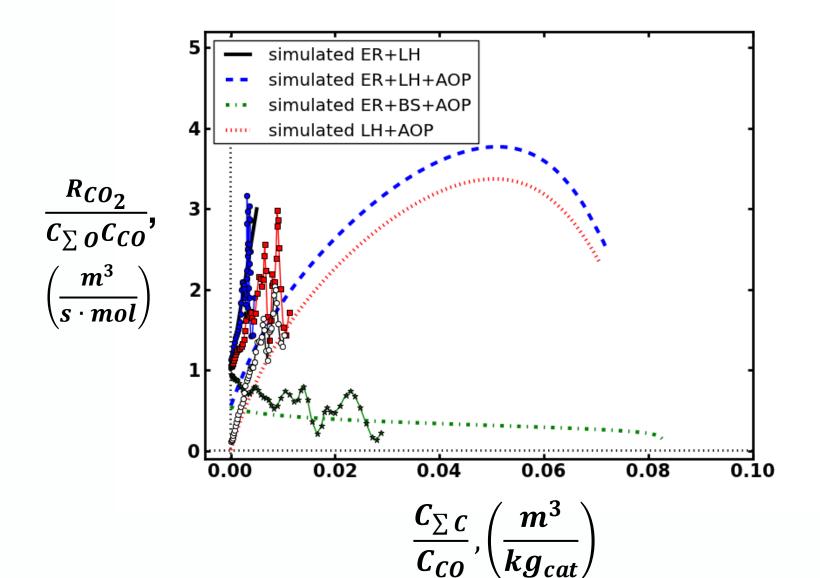
LH - Langmuir-Hinshelwood OAP -Oxygen Additional Process Buffer - spectator CO



### Decision tree



## Noise challenge



71

# "Stop time, thou art so beautiful!"

("Faust", Goethe)

## Goethe, "Faust"

"Werd ich zum Augenblicke sagen: Verweile doch: du bist zu schoen Dann magst du mich in Fesseln schlagen, Dann will ich gern zugrude gehn".

## **Difference from the Faust's strategy**

## In chemical time studies, we would like to stop any moment of time, not just the beautiful one.

#### **TAP-results**

- About 20 machines working in the world
- About 10 research groups US-St. Louis, Houston Europe – Belgium, Ghent; Netherlands, Delft ; N. Ireland, UK, Belfast; Germany – Ulm, Rostock, Bohum; France –Lyon; Spain; Switzerland –Zuerich; Asia- Japan – Tokyo, Toyota City; Thailand – Bangkok.
  - Many catalytic reactions: oxidation of simple molecules, many reactions of complete and selective oxidation of hydrocarbons

## Conclusions

(1) Within the Chemical Calculus approach, we have presented a novel strategy for **discriminating between minimal catalytic mechanisms** from a pool of all possible elementary steps.

(2) There was developed an experimental method of testing the non-steady-state catalytic reaction using the method of insignificant perturbations (TAP-pulse response method using the thin-zone reactor

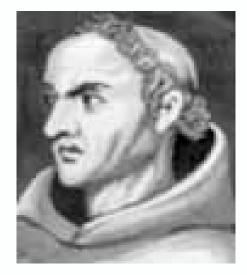
(3) There was developed a special procedure for extracting Rate, Concentrations and "Storages" of the non-steady-state catalyst.

(4) Testing the "rate-rate" and "rate-concentration" coherency is used for distinguishing the detailed mechanisms

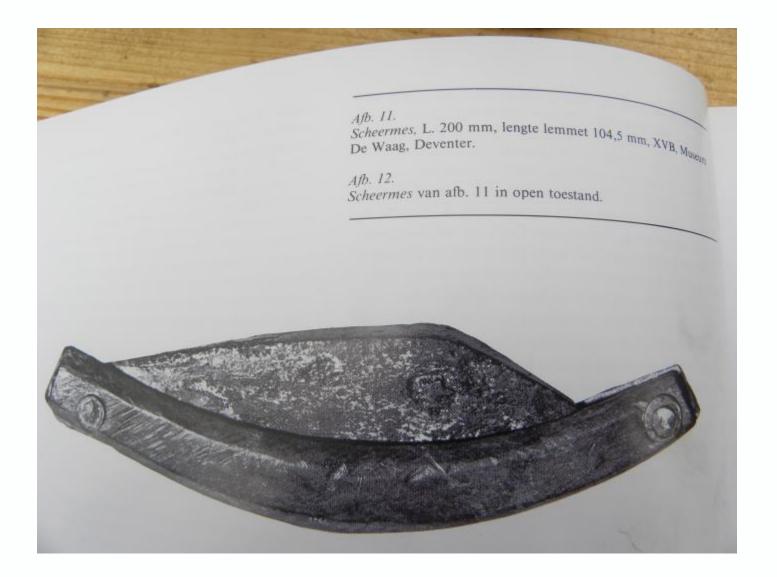
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#### Occam's razor



#### Occam's Razor

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#### **Origami Bonsai Tree as a Ideal Scientific Model**

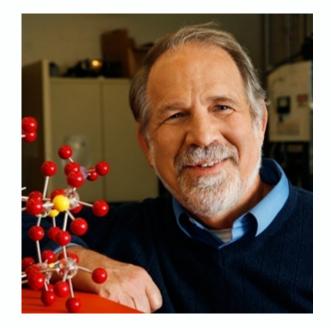


## Final step of modeling



"It has seen further it is by standing on the shoulders of giants" (Isaac Newton, Letter to Robert Hook, February 1676)

#### Prof. John T. Gleaves



#### Prof. Alexander Gorban



# **Gregory S. Yablonsky**



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- Long Term Structural Methusalem Funding by the Flemish Government